

A. Einstein:

(Vierteljahrsschrift für gerichtliche Medizin und öffentliches Sanitätswesen 44 (1912): 37-40.)

Gibt es eine Gravitationswirkung, die der elektrodynamischen Induktionswirkung analog ist?

<https://einsteinpapers.press.princeton.edu/vol4-doc/196>

HR: *he essentially derives **frame dragging**, which I do certainly not see as an analogy of gravitation and electromagnetism, see <http://henk-reints.nl/astro/HR-frame-dragging.pdf>.*

See also: <https://en.wikipedia.org/wiki/Gravitoelectromagnetism>

APOD 2011-05-10: "Gravity Probe B Confirms the Existence of Gravitomagnetism"

<https://apod.nasa.gov/apod/ap110510.html>

I will call it "gravitism".

<https://www.rs20.net/w/2012/08/how-do-magnets-work-magnetism-electrostatics-relativity/>

gives a comprehensible derivation of Ampère's law (basic magnetism) via Special Relativity.

Sir Isaac Newton:

PHILOSOPHIÆ NATURALIS PRINCIPIA MATHEMATICA.
LIBER TERTIUS: DE MUNDI SYSTEMATE.
REGULÆ PHILOSOPHANDI.

REGULA II.

*Ideoque effectuum naturalium ejusdem generis
eædem assignandæ sunt causæ, quatenus fieri potest.*

*Therefore natural effects of the same kind
must be assigned the same causes, as far as possible.*

HR:

similar things should be treated as similarly as achievable.

If magnetism is due to Lorentz contraction of a chain of electr. charged particles, then why wouldn't the very same apply to gravitation and a mass current?

Noticable difference: as far as we know, negative mass does not exist.

But let's give it a try:

Coulomb's law is <i>essentially identical</i> to Newton's law of gravitation:	
$F_e = k_C \frac{q_1 q_2}{r^2}$	$F_g = G \frac{m_1 m_2}{r^2}$
Maxwell (using k_C & c^2 instead of ϵ_0 & μ_0):	Reints (using G & c^2):
$k_C = \frac{1}{4\pi\epsilon_0} \therefore \frac{1}{\epsilon_0} = 4\pi k_C$	$\vec{A} :=$ gravitational field (<u>a</u> cceleration)
$c^2 = \frac{1}{\epsilon_0\mu_0} \therefore \mu_0 = \frac{4\pi k_C}{c^2}$	$\vec{Z} :=$ " gravitism " (equivalent of \vec{B})
$\nabla \cdot \vec{E} = \frac{\rho_q}{\epsilon_0} = 4\pi k_C \rho_q$	$\nabla \cdot \vec{A} = 4\pi G \rho_m \geq 0$
$\nabla \cdot \vec{B} = 0$	$\nabla \cdot \vec{Z} = 0$
$\nabla \times \vec{E} = \frac{\partial \vec{B}}{\partial t}$	$\nabla \times \vec{A} = \frac{\partial \vec{Z}}{\partial t}$
$\nabla \times \vec{B} = \mu_0 \left(\epsilon_0 \frac{\partial \vec{E}}{\partial t} + \vec{J} \right) = \frac{1}{c^2} \left(\frac{\partial \vec{E}}{\partial t} + 4\pi k_C \vec{J}_e \right)$	$\nabla \times \vec{Z} = \frac{1}{c^2} \left(\frac{\partial \vec{A}}{\partial t} + 4\pi G \vec{J}_m \right)$

Might "gravitism" have some physical meaning?

*Perfectly analogous equations **would** yield gravitational waves, just like EM, wouldn't they?*

dimensions / SI-units:	
$[B] = \frac{\text{N}}{\text{A}\cdot\text{m}} = \frac{\text{kg}}{\text{A}\cdot\text{s}^2} = \frac{\text{kg}}{\text{C}} \cdot \frac{1}{\text{s}}$	$[Z] = \frac{1}{\text{s}}$
Electron (lightest charged elementary particle): $W_e := m_e/e = 5.685\,630\,1036 \times 10^{-12} \text{ kg/C}$ $V_e = W_e c^2 = 510\,998.950\,00 \text{ J/C} \approx 511 \text{ kV}$ (not keV!)	<i>same dimension as Hubble constant</i>

magnetic force:	"gravitismic" force:
$F_B = q(\vec{v} \times \vec{B})$	$F_Z = m(\vec{v} \times \vec{Z}) = \vec{p} \times \vec{Z}$

Ampère's law in vacuum: (B around thin straight wire, I_e = electric current, SI: C/s)	"gravitismic" equivalent: (e.g. Z around a jet stream, I_m = mass current, SI: kg/s)
$B(r) = \frac{\mu_0 I_e}{2\pi r} = \frac{2k_C}{rc^2} I_e$	$Z(r) = \frac{2G}{rc^2} I_m$

Do you recognise (something like) the Schwarzschild radius?

Note: J (further above) = current density in {C|kg}/s/m², I = current in {C|kg}/s

What if:

we equate: $r = D_H$

and: $Z(r) = H = \frac{1}{t_H} \quad ?$

Well, it yields: $\frac{1}{t_H} = \frac{2G}{D_H c^2} I_m \quad \therefore I_m = \frac{D_H}{t_H} \cdot \frac{c^2}{2G} = c \frac{c^2}{2G}$

\therefore (?) current universal mass current:

$$I_m = \frac{c^3}{2G} \approx 2.01849 \times 10^{35} \text{ kg/s}$$

Found in <http://henk-reints.nl/astro/HR-Geometry-of-universe-slideshow.pdf> :

$$G = \frac{c^2 D_H}{2M_U}$$

yielding: $I_m = \frac{c^3}{2} \cdot \frac{2M_U}{c^2 D_H} = \frac{M_U c}{D_H} = \frac{M_U}{t_H}$

which equals the *mean Hubble flow* since the BB
(all mass left right here that long ago),

**but I draw no fundamental conclusions
from "what if" calculations.**

Nescio & hypothesefes non fingo.



Poynting vector:	Gravitational equivalent:
$\vec{S} = \vec{E} \times \vec{H}$ $\vec{B} = \mu_0 \mu_r \vec{H} = \frac{4\pi k_C}{c^2} \vec{H} \quad (\mu_r = 1)$ $\therefore \vec{H} = \frac{c^2}{4\pi k_C} \vec{B}$	
$\vec{S} = \frac{\vec{E} \times \vec{B}}{4\pi k_C} c^2$	$\vec{Y} = \frac{\vec{A} \times \vec{Z}}{4\pi G} c^2$
<p>\vec{S} is the local energy flux</p> <p>$\vec{S} = \dot{E}/A$ (energy flow per area)</p> <p>$\frac{\vec{E} \times \vec{B}}{4\pi k_C} = \text{eqv. mass flux, cf. } E = mc^2$</p>	$\kappa = \frac{8\pi G}{c^4} = \frac{2}{c^2} \cdot \frac{4\pi G}{c^2}$ <p>$c^2/2 = V_{r_S} = \text{abs. grav. pot. @ } r_S \text{ around any BH}^1$</p> $\therefore \frac{4\pi G}{c^2} = \kappa \frac{c^2}{2} = \kappa V_{r_S}$
$\frac{\left[\frac{\text{N}}{\text{C}} \right] \times \left[\frac{\text{kg}}{\text{C}\cdot\text{s}} \right]}{\left[\frac{\text{N}\cdot\text{m}^2}{\text{C}^2} \right]} = \left[\frac{\text{kg}}{\text{s}\cdot\text{m}^2} \right]$	$\vec{Y} = \frac{1}{\kappa V_{r_S}} \vec{A} \times \vec{Z}$

¹ BH = any mass that fits within its own Schwarzschild volume

Impedance of free space:	"Gravitismic impedance":
$Z_{0,e} = \sqrt{\mu_0/\epsilon_0} = \sqrt{\frac{4\pi k_C}{c^2} \cdot 4\pi k_C}$	
$Z_{0,e} = 4\pi k_C/c$ $\approx 376.730\ 313\ 668\ \Omega$ $[\Omega] = \left[\frac{\text{kg}\cdot\text{m}^2}{\text{A}^2\cdot\text{s}^3}\right] = \left[\frac{\text{kg}\cdot\text{m}^2}{\text{C}^2\cdot\text{s}}\right] = \left[\frac{\text{kg}}{\text{C}} \cdot \frac{\text{m}^2}{\text{C}\cdot\text{s}}\right]$	$Z_{0,g} = 4\pi G/c$ $\approx 2.79766 \times 10^{-18} \frac{\text{m}^2}{\text{kg}\cdot\text{s}}$
$\vec{H} = \frac{\vec{B}}{\mu_0} = \frac{c^2 \vec{B}}{4\pi k_C}$	$\vec{X} = \frac{c^2 \vec{Z}}{4\pi G}$
$Z_{0,e} = \frac{ \vec{E} }{ \vec{H} }$	$Z_{0,g} = \frac{ \vec{A} }{ \vec{X} }$
$ \vec{E} = \frac{4\pi k_C}{c} \vec{H} $	$ \vec{A} = \frac{4\pi G}{c} \vec{X} $

Universal mass/charge ratio:

$$k_C/G \approx \frac{8.987\,551\,7923 \times 10^9 \text{ N}\cdot\text{m}^2/\text{C}^2}{6.674\,30 \times 10^{-11} \text{ N}\cdot\text{m}^2/\text{kg}^2} \approx 1.346\,59 \times 10^{20} \text{ kg}^2/\text{C}^2$$

$$W_U := \sqrt{k_C/G} \approx \mathbf{1.160\,43 \times 10^{10} \text{ kg/C} \approx \mathbf{1.859\,21 \text{ }\mu\text{g/e}}$$

$$\approx 0.068\,1589 \text{ } m_{SC}/e \text{ }^{[2]} \quad \triangleq 167.097 \text{ MJ/e}$$

Fundamental constant of nature, relating mass/energy & electric charge.

$1/W_U$	$\approx 8.617\,52 \times 10^{-11} \text{ C/kg}$	$\approx \mathbf{14.6716}$	e/m_{SC}
	$\approx 9.588\,28 \times 10^{-28} \text{ C/J}$	$\approx 5.984\,53 \times 10^{-9}$	e/J
	$\approx 7.560 \times 10^{42} \text{ C}/M_U$	$\approx 4.718 \times 10^{61}$	e/M_U
	$\approx 1.462 \times 10^{-78} \text{ C}/\Delta m_u$	$\approx 9.124 \times 10^{-60}$	$e/\Delta m_u$
		$\approx 8.200 \times 10^{-43}$	$e/\Delta E_u$ [3]

Intrinsic cosmic electric potential: $V_{e,U} = W_U c^2 \approx 1.042\,94 \times 10^{27} \text{ volts.}$

I have no idea what these values would actually mean.

I refuse to believe the cosmos would be electrically charged or so.

$$W_p = m_p/e \approx 1.043\,97 \times 10^{-8} \text{ kg/C} \quad \triangleq 1.503\,28 \times 10^{-10} \text{ J/e}$$

$$W_e = m_e/e \approx 5.685\,63 \times 10^{-12} \text{ kg/C} \quad \triangleq 8.187\,11 \times 10^{-14} \text{ J/e}$$

² m_{SC} = mass for which $2r_s = \lambda_c$ ("Compton dipole" inside Schwarzschild sphere) $\approx 27.277\,51 \text{ }\mu\text{g}$

³ See <http://henk-reints.nl/astro/HR-Geometry-of-universe-slideshow.pdf>

Because I see no reason why e or m_{SC} would be (Hubble) time dependent, I consider both to be very fundamental units.

Therefore I consider: $1/W_U \approx 14.6716 e/m_{SC}$ just as fundamental a quantity as well (accuracy restricted to min. of k_C and G , which is 6 digits)

Just some trial calculations:

$$14.6716 \cdot \alpha \approx 0.107064$$

$$14.6716/\alpha \approx 2010.54$$

Both seem nothing special to me.

Radiation by electric dipole:

[https://phys.libretexts.org/Bookshelves/Electricity and Magnetism/Essential Graduate Physics - Classical Electrodynamics \(Likharev\)/08%3ARadiation Scattering Interference and Diffraction/8.02%3A Electric Dipole Radiation](https://phys.libretexts.org/Bookshelves/Electricity_and_Magnetism/Essential_Graduate_Physics_-_Classical_Electrodynamics_(Likharev)/08%3ARadiation_Scattering_Interference_and_Diffraction/8.02%3A_Electric_Dipole_Radiation) :

8.2: Electric Dipole Radiation - Ph
x

← → ↻ 🏠 🔒 [phys.libretexts.org/Bookshelves/Electricity_and_Magnetism/Essential_Graduate_Physics_-_Classical_Electrodynamics_\(Likharev\)/08%3ARadiation_Scattering_In...](https://phys.libretexts.org/Bookshelves/Electricity_and_Magnetism/Essential_Graduate_Physics_-_Classical_Electrodynamics_(Likharev)/08%3ARadiation_Scattering_In...)
🔍 ⚙️ 🗑️ 📄 HR ⋮

Far-field wave
$$\mathbf{B}(\mathbf{r}, t) = \frac{\mu}{4\pi r} \nabla \times \dot{\mathbf{p}} \left(t - \frac{r}{\nu} \right) = -\frac{\mu}{4\pi r \nu} \mathbf{n} \times \ddot{\mathbf{p}} \left(t - \frac{r}{\nu} \right). \quad (8.24)$$

This expression means that the magnetic field, at the observation point, is perpendicular to the vectors \mathbf{n} and (the retarded value of) $\ddot{\mathbf{p}}$, and its magnitude is

$$B = \frac{\mu}{4\pi r \nu} \ddot{p} \left(t - \frac{r}{\nu} \right) \sin \Theta, \quad \text{i.e. } H = \frac{1}{4\pi r \nu} \ddot{p} \left(t - \frac{r}{\nu} \right) \sin \Theta, \quad (8.25)$$

where Θ is the angle between those two vectors – see Fig. 2.⁷

Fig. 8.2. Far-fields of a localized source, contributing to its electric dipole radiation.

The most important feature of this result is that the time-dependent field decreases very slowly (only as $1/r$) with the distance from the source, so that the radial component of the corresponding Poynting vector (7.9b),⁸

$$S_r = ZH^2 = \frac{Z}{(4\pi r \nu)^2} \left[\ddot{p} \left(t - \frac{r}{\nu} \right) \right]^2 \sin^2 \Theta, \quad \text{Instant power density} \quad (8.26)$$

Assuming: dipole moment = $p = qd \sin \omega t \therefore \ddot{p} = -qd\omega^2 \sin \omega t$

we find: $H_{\theta=90^\circ} = \frac{\ddot{p}(t-r/c)}{4\pi r c} = \frac{-qd\omega^2}{4\pi r c} \sin \omega(t - r/c)$

and: amplitude of $(\vec{E} \triangleq Z_{0,e}\vec{H})$: $\frac{k_C q d \omega^2}{r c^2}$

as well as: $S_r = Z_{0,e} H^2 = \frac{4\pi k_C}{c} \left(\frac{-qd\omega^2}{4\pi r c} \sin \omega(t - r/c) \right)^2$
 $= \frac{k_C q^2 d^2 \omega^4}{4\pi r^2 c^3} \sin^2 \omega(t - r/c)$

Mean radial energy flux in equatorial plane of dipole: $\overline{S_r} = \frac{k_C q^2 d^2 \omega^4}{8\pi r^2 c^3}$

Gravitismic equivalent:

Amplitude of \vec{A} : $\frac{G m d \omega^2}{r c^2}$

Mean equatorial radial energy flux: $\overline{Y_r} = \frac{G m^2 d^2 \omega^4}{8\pi r^2 c^3}$

<https://andrealommen.github.io/PHY309/lectures/dipole> :

Total radiated power, integrated over entire sphere around dipole antenna:

$$P = \frac{\mu_0 p_0^2 \omega^4}{12\pi^2 c} = \frac{4\pi k_C \cdot p_0^2 \omega^4}{c^2 \cdot 12\pi^2 c} = \frac{k_C q^2 d^2 \omega^4}{3\pi c^3}$$

Gravitismic equivalent:

$$P = \frac{G m^2 d^2 \omega^4}{3\pi c^3}$$

And now, something completely different:

<https://astronomy.swin.edu.au/cosmos/g/gravitational+waves> :

The power emitted by a binary system of masses m_1 and m_2 in a circular orbit at a distance d from each other in gravitational waves is:

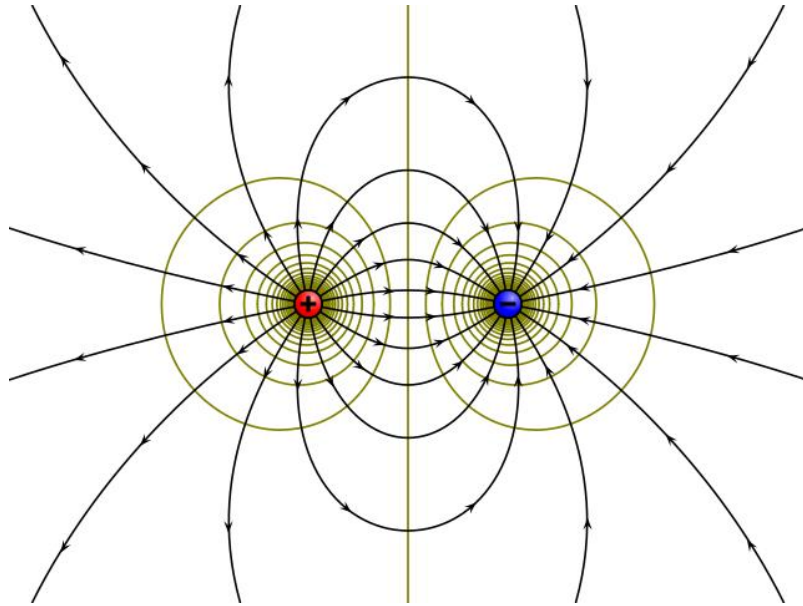
$$P = \frac{32G^4}{5c^5 d^5} (m_1 m_2)^2 (m_1 + m_2)$$

$$m_1 = m_2 = m \Rightarrow P = \frac{32G^4}{5c^5 d^5} \cdot 2m^5 = \frac{64G^4}{5} \left(\frac{m}{cd}\right)^5 \quad \text{🤔}$$

Ergo: the e-dipole equivalent is a miserable failure.

Note: energy manifests as mass, not as charge, & charge can be \pm .

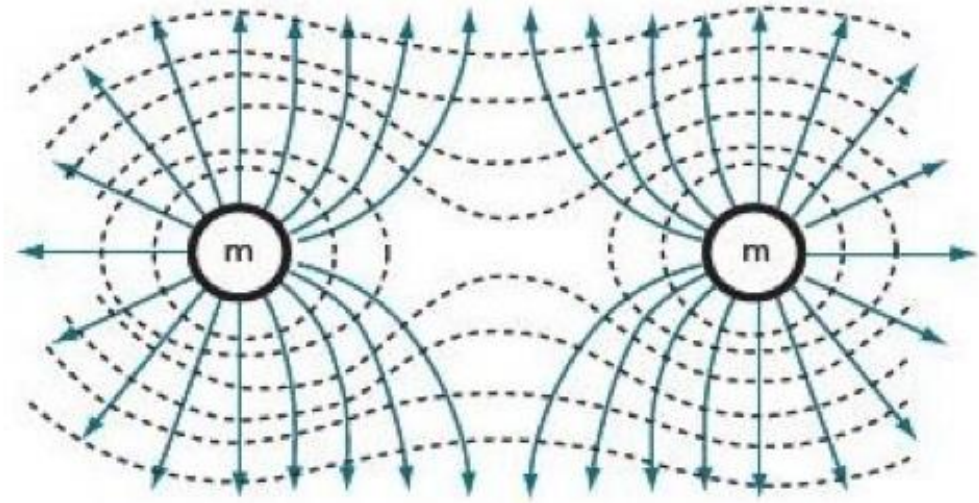
Electric dipole field & equipotentials:



<https://commons.wikimedia.org/wiki/File:Electric-dipole-field-lines-and-equipotential-lines.svg>

Same sign: repulsive.

Gravitational dipole field & equipotentials:



<https://sites.google.com/site/ibdpphysics101/course-units/10-fields/10-1-describing-fields>

Same sign: attractive.

Magnetic dipole:

circular electric current I_e around surface $A = \pi r_e^2$

magnetic moment: $\mathfrak{m} = I_e A = \pi I_e r_e^2$

magnetic flux for $r_e \rightarrow 0$ preserving \mathfrak{m} :

$$\vec{B}(r) = \frac{\mu_0}{4\pi} \left[\frac{3\vec{r}(\vec{\mathfrak{m}} \cdot \vec{r})}{r^5} - \frac{\vec{\mathfrak{m}}}{r^3} \right] = \frac{k_C}{c^2} \frac{3\hat{r}(\vec{\mathfrak{m}} \cdot \hat{r}) - \vec{\mathfrak{m}}}{r^3}$$

in the (equatorial) plane of: I_e , with $r \gg r_e$:

$$\vec{\mathfrak{m}} \perp \hat{r} \Rightarrow \vec{\mathfrak{m}} \cdot \hat{r} = 0, \quad B = |\vec{B}| = \frac{-k_C \mathfrak{m}}{c^2 r^3} \quad (\text{sign indicates direction opposite to } \vec{\mathfrak{m}})$$

Gravitismic equivalent:

two equal masses m , orbiting each other at r_{orb} :

$$\text{Kepler III: } T_{\text{orb}} = \sqrt{\frac{4\pi^2 r_{\text{orb}}^3}{Gm_{\text{tot}}}} = \sqrt{\frac{2\pi^2 r_{\text{orb}}^3}{Gm}} \therefore I_m = \frac{2m}{T_{\text{orb}}} = \frac{m}{\pi} \sqrt{\frac{2Gm}{r_{\text{orb}}^3}}$$

$$\text{gravitismic moment: } \mathfrak{g} = \pi I_m r_{\text{orb}}^2 = \pi \frac{m}{\pi} \sqrt{\frac{2Gm}{r_{\text{orb}}^3}} r_{\text{orb}}^2 = \sqrt{2Gr_{\text{orb}} m^3}$$

$$\text{equatorial gravitismic flux: } Z(r \gg r_{\text{orb}}) = \frac{-G\mathfrak{g}}{c^2 r^3} = \frac{-\sqrt{2r_{\text{orb}}(Gm)^3}}{c^2 r^3}$$

$$Gm = \frac{r_S c^2}{2} \therefore \mathbf{Z}(\mathbf{r}) = \frac{-\sqrt{2r_{\text{orb}} r_S^3 c^6 / 8c^4}}{r^3} = \frac{-\sqrt{r_{\text{orb}} r_S^3 c^2 / 4}}{r^3} = \frac{-c}{2} \cdot \frac{\sqrt{r_{\text{orb}} r_S^3}}{r^3}$$

Recapitulation:

Electromagnetism:		Gravitism:
$k_C, \vec{E}, \vec{B}, \vec{H}, \vec{S}$	\cong	$G, \vec{A}, \vec{Z}, \vec{X}, \vec{Y}$
$\epsilon_0 = \frac{1}{4\pi k_C}, \mu_0 = \frac{4\pi k_C}{c^2}$		
$\vec{H} = \frac{\vec{B}}{\mu_0} = \frac{c^2 \vec{B}}{4\pi k_C}$		$\vec{X} = \frac{c^2 \vec{Z}}{4\pi G}$
$Z_{0,e} = \sqrt{\frac{\mu_0}{\epsilon_0}} = \mu_0 c = \frac{4\pi k_C}{c}$		$Z_{0,g} = \frac{4\pi G}{c}$
$ \vec{E} = \frac{4\pi k_C}{c} \vec{H} $		$ \vec{A} = \frac{4\pi G}{c} \vec{X} $
$\vec{S} = \vec{E} \times \vec{H} = \frac{c^2}{4\pi k_C} (\vec{E} \times \vec{B})$		$\vec{Y} = \vec{A} \times \vec{X} = \frac{c^2}{4\pi G} (\vec{A} \times \vec{Z})$
$S_r = Z_{0,e} H^2 = \frac{4\pi k_C}{c} \left(\frac{c^2 B}{4\pi k_C} \right)^2 = \frac{c^3 B^2}{4\pi k_C}$		$Y_r = Z_{0,g} X^2 = \frac{4\pi G}{c} \left(\frac{c^2 Z}{4\pi G} \right)^2 = \frac{c^3 Z^2}{4\pi G}$
$F_B = q(\vec{v} \times \vec{B})$		$F_Z = m(\vec{v} \times \vec{Z}) = \vec{p} \times \vec{Z}$
$B(r) = \frac{\mu_0 I_e}{2\pi r} = \frac{2k_C}{rc^2} I_e$		$Z(r) = \frac{2G}{rc^2} I_m$

Now I unfoundedly presume the non-oscillating dipole yields an EM-like grav. wave...

Suppose: $r_{\text{orb}} = r_{\text{ISCO}} = 3r_S$ then: $Z(r) = \frac{-c}{2} \cdot \frac{\sqrt{3r_S r_S^3}}{r^3} = \frac{-cr_S^2 \sqrt{3}}{2r^3}$

($Z(r)$ was derived using Newtonian gravitation, so this is an itsy bitsy tricky...)

suppose as well: 2 instances of Sgr A* orbiting each other in the galactic plane,
each has: $M \approx 8.26 \times 10^{36} \text{ kg}$

Sgr A* distance: $r \approx 26670 \text{ ly} \approx 2.523 \times 10^{20} \text{ m}$

gravitismic flux: $Z \approx -2.433 \times 10^{-33} \text{ s}^{-1}$

cf. Hubble constant: $H \approx 2.3 \times 10^{-18} \text{ s}^{-1} \approx 71 \text{ km/s/Mpc}$

gravitational field of wave: $|\vec{A}| = \frac{4\pi G}{c} |\vec{Z}| \approx -6.8 \times 10^{-51} \text{ m}^2 \text{ kg}^{-1} \text{ s}^{-2}$

momentum of sun in its galactic orbit (i.e. around those 2 Sgr A*):

$$\vec{p} \approx M_{\odot} \vec{v}_{\odot} \approx 4.375 \times 10^{35} \text{ kg m/s}$$

gravitismic force: $\vec{F}_Z = \vec{p} \times Z \approx -1065 \text{ N}$

Equatorial energy flux: $Y_r = \frac{c^3 Z^2}{4\pi G} = \frac{3c^5 r_S^4}{16\pi G r^6} = \frac{3c^5 \cdot 16G^4 M^4}{16\pi G r^6 c^8} = \frac{3G^3 M^4}{\pi c^3 r^6} \approx 1.9 \times 10^{-31} \text{ W/m}^2$

Einstein's GR: $P_{\text{tot}} = \frac{64G^4}{5} \left(\frac{M}{cd}\right)^5$, $d = 3 \frac{2GM}{c^2} \therefore \frac{M}{cd} = \frac{c}{6G} \therefore P_{\text{tot}} = \frac{2c^5}{1215G} \approx 5.97 \times 10^{49} \text{ W}$

(homogeneous) mean flux: **EARTHQUAKE ALARM:** $j_{\text{grav}} = \frac{P_{\text{tot}}}{4\pi r^2} \approx 75 \times 10^{+6} \text{ W/m}^2$

